

**Semester Two Examination, 2020**

**Question/Answer Booklet**

**MATHEMATICS**

**METHODS**

**ATAR Year 12**

**Section One:**

**Calculator-free**

Student Name: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

Please circle your teacher’s name

**Teacher: Miss Long Miss Rowden Ms Stone**

**Time allowed for this paper**

Reading time before commencing work: 5 minutes

Working time for paper: 50 minutes

**Materials required/recommended for this paper**

***To be provided by the supervisor***

Number of additional

answer booklets used

(if applicable):

This Question/Answer Booklet

Formula Sheet

***To be provided by the candidate***

Standard items: pens (blue/black preferred), pencils (including coloured), sharpener, correction fluid/tape, eraser, ruler, highlighters

Special items: nil

**Important note to candidates**

No other items may be taken into the examination room. It is **your** responsibility to ensure that you do not have any unauthorised material. If you have any unauthorised material with you, hand it to the supervisor **before** reading any further.

**Structure of this paper**

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| Section | Number of questions available | Number of questions to be answered | Suggested working time (minutes) | Marks available | Percentage of examination |
| Section One: Calculator free | 8 | 8 | 50 | 52 | 35 |
| Section Two:Calculator-assumed | 13 | 13 | 100 | 98 | 65 |
|  |  |  |  | **Total** | 100 |

**Instructions to candidates**

1. The rules for the conduct of the ATAR course examinations are detailed in the *Year 12 Information Handbook 2020*. Sitting this examination implies that you agree to abide by these rules.
2. Write your answers in this Question/Answer booklet.
3. You must be careful to confine your answers to the specific questions asked and to follow any instructions that are specific to a particular question.
4. Supplementary pages for the use planning/continuing your answer to a question have been provided at the end of the Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.
5. Show all your working clearly. Your working should be in sufficient detail to allow your answers to be checked readily and for marks to be awarded for reasoning. Incorrect answers given without supporting reasoning cannot be allocated any marks. For any question or part question worth more than two marks, valid working or justification is required to receive full marks. If you repeat any question, ensure that you cancel the answer you do not wish to have marked.
6. It is recommended that you do not use pencil, except in diagrams.
7. The Formula sheet is not to be handed in with your Question/Answer booklet.

**Section One: Calculator-free 35% (52 Marks)**

This section has eight (8) questions. Answer **all** questions. Write your answers in the spaces

provided.

Supplementary pages for the use of planning/continuing your answer to a question have been provided at the end of this Question/Answer booklet. If you use these pages to continue an answer, indicate at the original answer where the answer is continued, i.e. give the page number.

Working time: 50 minutes.

Question 1 (7 marks)

(a) Determine an expression for when

(i) . (2 marks)

(ii) . (3 marks)

(b) For the positive number , let .

Determine the value(s) of for which . (2 marks)

Question 2 (7 marks)

The discrete random variable is defined by

(a) Determine the value of the constant . (2 marks)

(b) Determine

(i) . (1 mark)

(ii) . (2 marks)

(iii) . (2 marks)

Question 3 (5 marks)

The rate of change of pressure in an air tank is given by , where is the time in minutes since it began emptying from an initial pressure of psi.

(a) Determine an expression for the pressure in the tank at any time . (2 marks)

(b) Determine

1. the time taken for the pressure in the tank to fall to psi. (2 marks)

(ii) the minimum pressure in the tank for . (1 mark)

Question 4 (6 marks)

The continuous random variable takes values in the interval to and has **cumulative** distribution function where

(a) Determine

(i) . (1 mark)

(ii) the value of , if . (2 marks)

(b) Determine , the probability density function of , and sketch the graph of .

 (3 marks)

Question 5 (7 marks)

The function is defined by .

The second derivative of is .

Determine the coordinates and nature of all stationary points of the graph of .

Question 6 (7 marks)

(a) Determine the value of . (2 marks)

(b) Given that , determine the value of . (2 marks)

(c) Determine the solution to the equation in the form . (3 marks)

Question 7 (6 marks)

The acceleration at time seconds of a small body travelling in a straight line is given by

When the body was at the origin and seconds later its displacement was cm.

Determine the velocity of the body when .

Question 8 (7 marks)

The graph and a table of values for is shown below, where .



Let .

(a) By using the information shown and considering sums of the form explain why .

 (3 marks)

(b) In a similar manner to (a), determine the lower estimate,, for the value of .

 That is, the value of for which .

(2 marks)

(c) Use your previous answers to determine a numerical estimate for and explain whether your estimate is smaller or larger than the exact value of . (2 marks)

Supplementary page

Question number: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_

Supplementary page

Question number: \_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_\_